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GENERALIZED DEGREE BASED DOMINATION IN GRAPHS

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Abstract

In this article, we initiate a new concept, which is the amalgamation of both domination theory and the degree-based topological indices in the name of a k-degree based domination related parameters of a graph. Here, we investigate several properties, bounds, and characterizations of these newly introduced parameters.

Keywords and phrases: Zagreb index, dominating set, first Zagreb dominating set, first strong Zagreb dominating set, first weak Zagreb dominating set.

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