

COMPACT HARMONIC FINSLER MANIFOLDS WITH FINITE FUNDAMENTAL GROUPS

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Abstract

We prove that compact harmonic reversible Finsler manifolds with finite fundamental groups must be Riemannian.

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