

## HOMOTOPIES TO DIFFEOMORPHISMS IN FIELD THEORY

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### Abstract

Considering homotopies between non-compact Lagrangian submanifolds, and using the Fukaya conjecture relative to the Witten deformation of higher product structures (conforming a Fukaya category from the perspective of the Floer complexes) are determined diffeomorphisms  $C_{-*}(\Omega_\chi) \rightarrow \mathcal{W}(H)$ , whose space of paths go from  $\gamma(\chi)$ , to  $\phi(\chi)$ , foreseen in  $HW^*(L_0, L_1) \cong H_*(\mathcal{P}_{\chi_0, \chi_1})$ . Then the field ramification of the space  $C_{-*}(\Omega_\chi)$  is a connection obtained under the following category scheme:

$$\begin{array}{ccc}
 \text{mod}(B) & \xrightarrow{\mathcal{R}^{-1}} & C \\
 \nearrow \downarrow & & \nearrow \downarrow \\
 0_c(\phi) \in H(\text{mod}f(C_{-*}(\Omega Z))) & \rightarrow & H(\mathcal{M})\mathcal{M} \\
 \downarrow \nearrow \Omega Z & \rightarrow & \downarrow \text{embb} \nearrow \\
 C_{-*}(\Omega_\chi) & \xrightarrow{\text{Diff}} & \mathcal{W}(H) \ni \phi
 \end{array}$$

**Keywords and phrases:** Fukaya category, homotopy, Lagrangian submanifolds, non-commutative rings, topological diffeomorphisms, wrapped Floer cohomology.

Received March 9, 2022

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