

## ASYMPTOTIC EXPANSIONS FOR ELLIPTIC BOUNDARY VALUE PROBLEMS

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### Abstract

We propose an asymptotic solution related to a Cauchy problem for an elliptic equation or system with data on a part of the boundary within solving operators of Zaremba type mixed boundary problems.

**Keywords and phrases:** nonlinear PDE, Cauchy problem, variational problems, elliptic operators.

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